

# Symmetric Key Cryptography

PQCRYPTO Summer School on Post-Quantum  
Cryptography 2017

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# Introduction to Symmetric Key Cryptography

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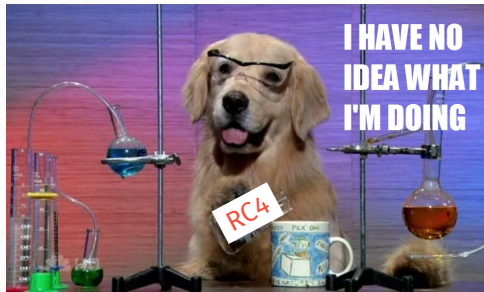
Where does security fail?

- 
- 
- 
-

# Symmetric Key Cryptography

Where does security fail?

- User
- 
- 
- 



Don't blame the user!

Where does security fail?

- User
- Implementation
- 
- 



Heartbleed

Where does security fail?

- User
- Implementation
- Protocols
- 



Drown Attack

# Symmetric Key Cryptography

Where does security fail?

- User
- Implementation
- Protocols
- Cryptographic Algorithms

## Myth

"Cryptographic Algorithms are *never* the weakest link."

## Hash Function MD5

- Not collision resistant [WY05]
- Constructing a rogue CA [Ste+09]

## Hash Function SHA-1

- Not collision resistant [WYY05]
- First practical collisions this year

## Stream Cipher RC4

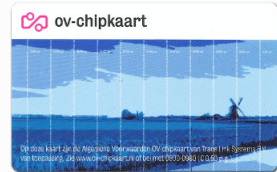
- Plaintext Recovery in TLS [ALF+13]
- ...



# Symmetric Key Cryptography

A long list...

- MIFARE Classic (Crypto 1)
- Keeloq
- A5/1, A5/2
- DECT
- Kindle Cipher
- ...



# Symmetric Key Cryptography

What can we do?

- Encryption
- Authentication (MAC)
- Hashing
- Random Number Generation
- Digital Signature Schemes
- Key Exchange



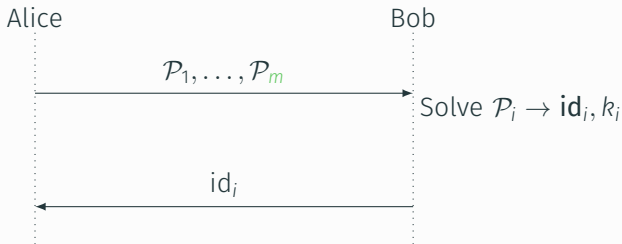
## Digital Signatures

- Hash-based Signature Schemes (MSS, XMSS [BDH11], SPHINCS [Ber+15])
- Zero-Knowledge Proof Based (Fish [Cha+17], Picnic [Cha+17])

# Symmetric Key Cryptography

## Key Exchange with Merkle Puzzles (1978)

- Alice prepares  $m$  Puzzles:  $\mathcal{P}_1, \dots, \mathcal{P}_m$ .
- Solving a puzzle requires  $n$  steps.
- Reveals an id and key  $k_{id}$ .

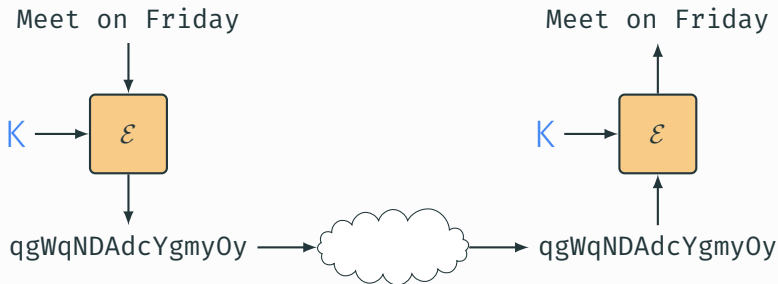


- Bob needs to compute  $n$  steps.
- Adversary needs to compute  $mn$ .

# Symmetric Key Cryptography

## Note

We need a **shared** secret between the parties.



# Symmetric Key Cryptography

The adversary

- Eavesdrop on communication
- Modify transmission
- Delete/Insert messages
- ...

...but is bound in

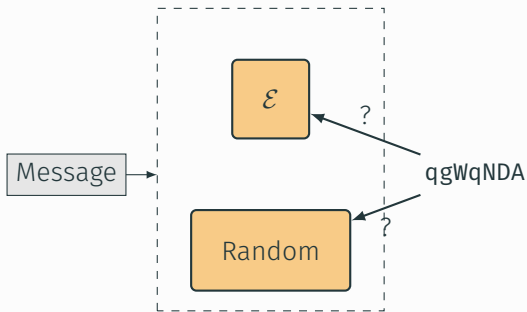
- Computational power
- Available memory
- Time
- Data



# Symmetric Key Cryptography

## Goals of the attacker

- Decrypt a ciphertext
- Forge a signature
- Recover the secret key
- Distinguish output
- ...



# Symmetric Key Cryptography

How do we achieve security for an algorithm?

- Reduce security to a *hard* problem.
- Make it secure against all known attacks.

## Note

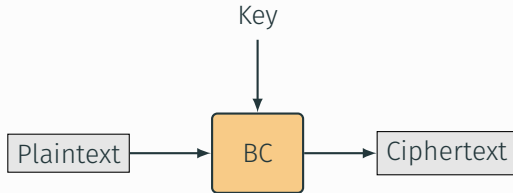
We can **not** proof security for a primitive.



# Encryption

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# Block Ciphers

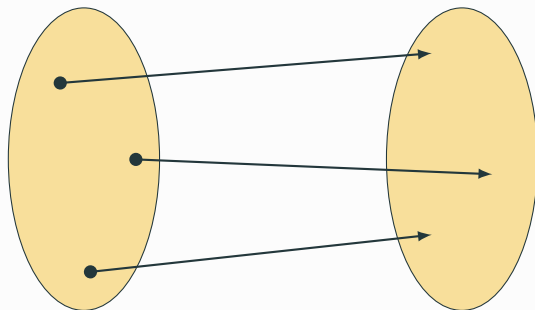


- Encrypts blocks of fixed size  $n$  with a key of size  $k$ .
- Requires a mode to encrypt arbitrary messages.

Block cipher is not an encryption scheme

# Symmetric Key

## Ideal Block Cipher



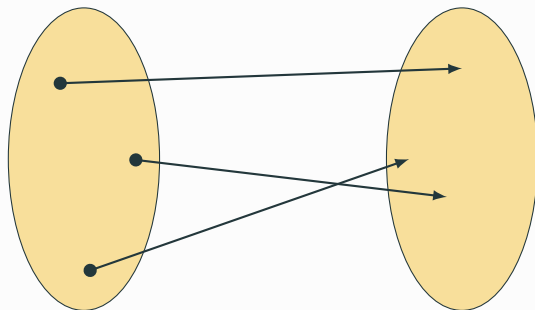
Plaintexts

Ciphertexts

$K = 101010111010\dots$

# Symmetric Key

## Ideal Block Cipher



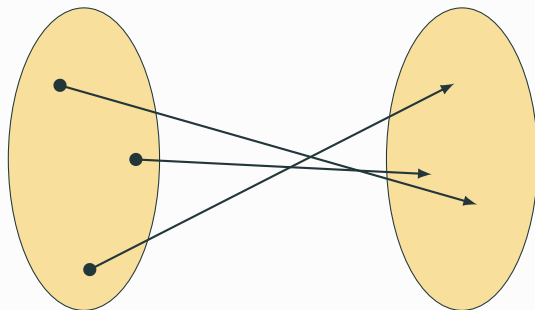
Plaintexts

Ciphertexts

$K = 001111110000\dots$

# Symmetric Key

## Ideal Block Cipher



Plaintexts

Ciphertexts

$K = 111111001000\dots$

A block cipher can be seen as a family of  $2^k$   $n$ -bit bijections.

## Problem

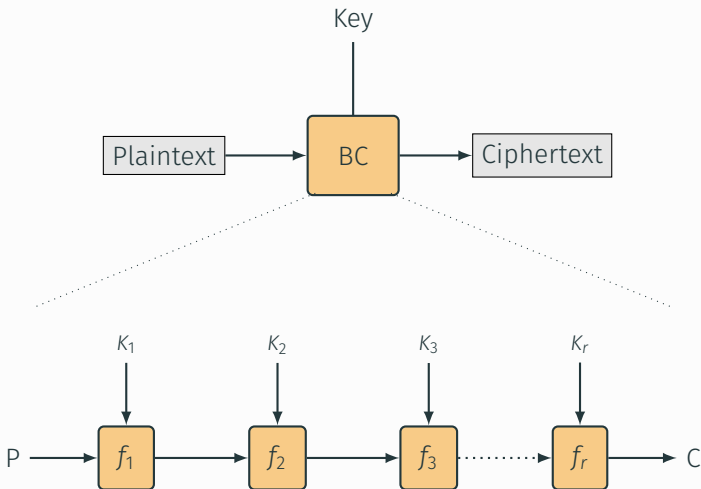
There are  $2^n!$  bijections, we ideally want to choose  $2^k$  uniformly at random.

## Goal

We need something **efficient** to mimic this behaviour.

# Block Ciphers

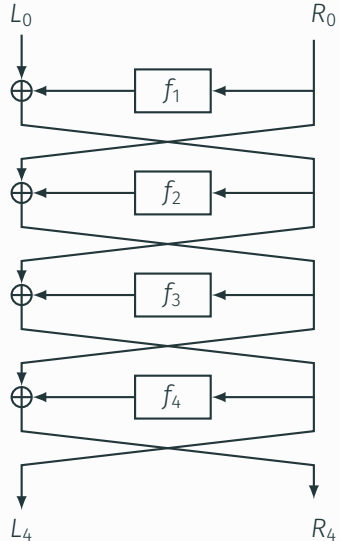
## Iterated construction



# Symmetric Key Cryptography

## The Data Encryption Standard

- Developed in 1970s at IBM.
- Feistel Network with 16 rounds.
- Encrypts 64-bit blocks with **56-bit** keys.
- Standardized in 1977.





## The Advanced Encryption Standard (AES)

- Public Competition hosted by NIST (1997-2001)
- Must support block size of 128 bits and key size of 128, 192 and 256 bits.

- |            |           |            |
|------------|-----------|------------|
| • CAST-256 | • FROG    | • RC6      |
| • CRYPTON  | • HPC     | • Rijndael |
| • DEAL     | • LOKI97  | • SAFER+   |
| • DFC      | • MAGENTA | • Serpent  |
| • E2       | • MARS    | • Twofish  |

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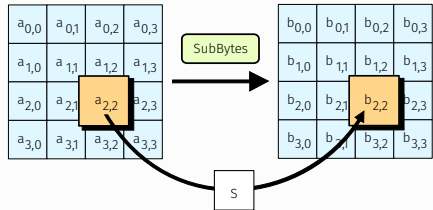
## AES/Rijndael

- Blocksize: 128-bit
- Keysize: 128/192/256 bits
- Iterated block cipher with 10/12/14 rounds
- Is part of a wide-range of standards.
- Direct support by instructions in modern CPUs.

# Block Ciphers

Update  $4 \times 4$  state of bytes

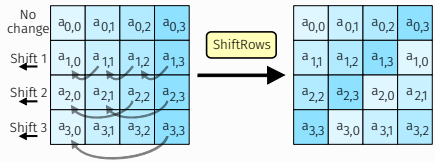
- SubBytes
- ShiftRows
- MixColumns
- AddKey



# Block Ciphers

Update  $4 \times 4$  state of bytes

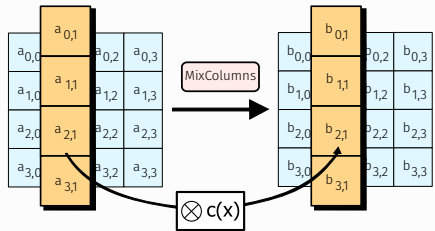
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# Block Ciphers

Update  $4 \times 4$  state of bytes

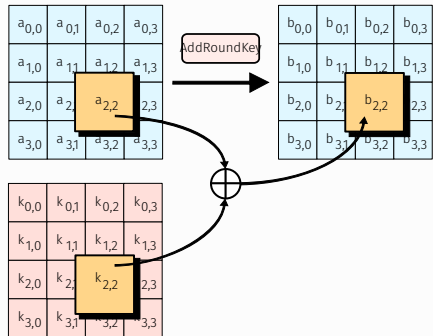
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# Block Ciphers

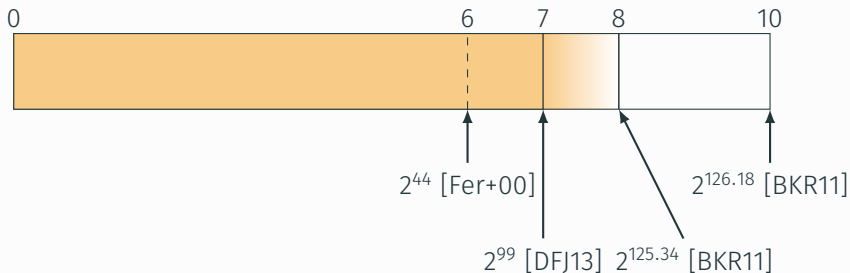
Update  $4 \times 4$  state of bytes

- SubBytes
- ShiftRows
- MixColumns
- AddKey



# Block Ciphers

Current state of key recovery attacks for AES-128



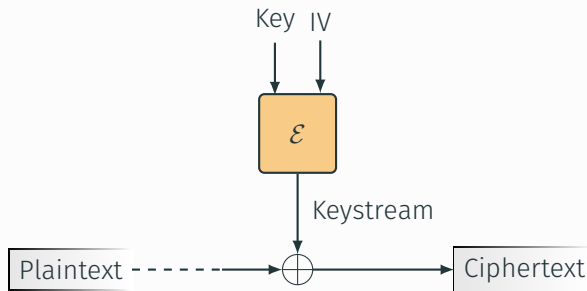
There are many more attacks with different trade-offs of time/data/memory.



# Stream Ciphers

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# Stream Ciphers



- Encrypts individual *digits*.
- IV to have multiple key stream for each K
- Requires no padding.
- Often used for low-bandwidth communication.

Widely found in practice

- GSM standard (A5/1, A5/2)
- LTE (SNOW 3G, ZUC)
- Bluetooth (E0)
- TLS protocol (RC4, ChaCha20)

## eSTREAM Project (EU)

### Goal

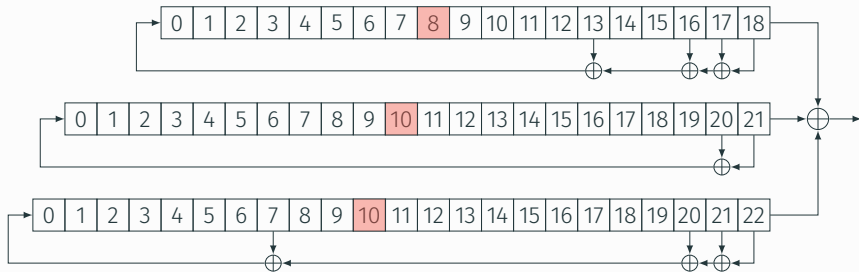
*...promote the design of efficient and compact stream ciphers suitable for widespread adoption...*

Software	Hardware
HC-128	Grain v1
Rabbit	MICKEY 2.0
Salsa20/12	Trivium
SOSEMANUK	

# Stream Ciphers

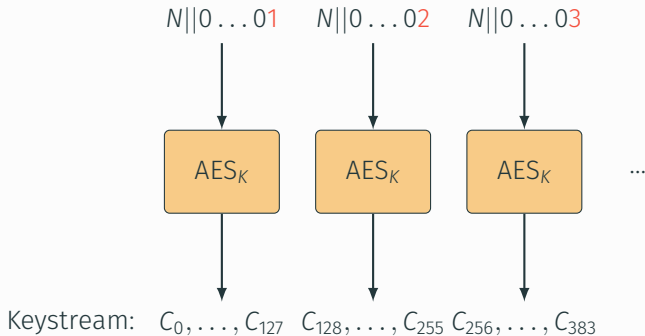
## LFSR-based Constructions, e.g. A5/1

- Load IV and Key in registers.
- Shift registers depending on values in  .
- Produces 1-bit output in each iteration.



# Stream Ciphers

## Counter Mode (CTR)



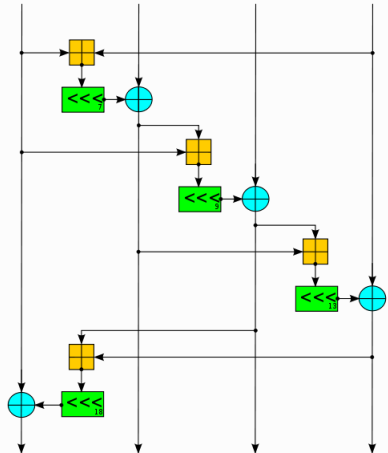
### Note

Reusing nonce and counter gives same keystream.

# Stream Ciphers

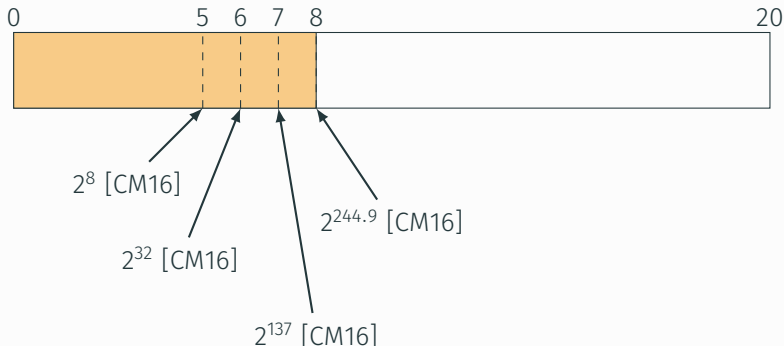
Salsa20 / ChaCha20

- ARX-based design
- 512-bit state
- Uses 256-bit key
- 20 rounds
- Fast in software
- ChaCha20-Poly1305 in TLS



# Stream Ciphers

Current state of key recovery attacks for Salsa20



For ChaCha typically one round less.

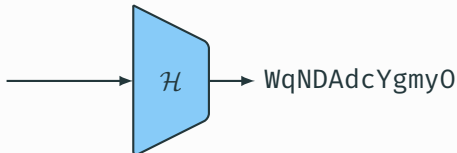


# Cryptographic Hash Functions

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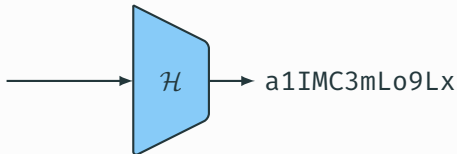
# Hash Functions

"There was of course no way of knowing whether you were being watched at any given moment. How often, or on what system, the Thought Police plugged in on any individual wire was guesswork. It was even conceivable that they watched everybody all the time. But at any rate they could plug in your wire whenever they wanted to. You had to live – did live, from habit that became instinct – in the assumption that every sound you made was overheard, and, except in darkness, every movement scrutinized."



# Hash Functions

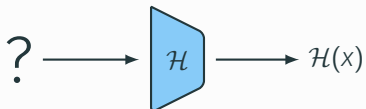
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## Applications

- Integrity Check
- Digital Signature Schemes (this afternoon)
- Password Hashing (<https://password-hashing.net/>)
- Message Authentication
- Commitment Schemes
- ...

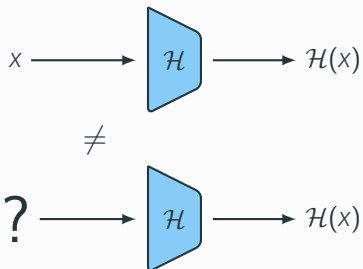
## Preimage Resistance



For  $n$ -bit output size

- Best attack:  $2^n$

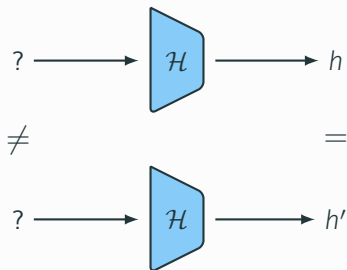
## Second-Preimage Resistance



For  $n$ -bit output size

- Best attack:  $2^n$

## Collision Resistance



For  $n$ -bit output size

- Best attack:  $2^{n/2}$

Hardness of finding collision vs. preimages in practice

Algorithm	Year	n	Collision	Preimage
MD4	1990	128	< 1 sec	
MD5	1992	128	< 1 sec	
SHA-1	1995	160	$2^{63}$	
SHA-256	2001	256	$2^{65.5}$ 31/64 rounds	

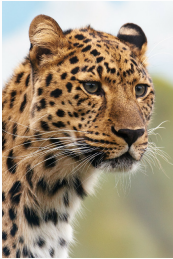


Hardness of finding collision vs. preimages in practice

Algorithm	Year	n	Collision	Preimage
MD4	1990	128	< 1 sec	$2^{78.4}$ [Guo+10]
MD5	1992	128	< 1 sec	$2^{123.4}$ [SA09]
SHA-1	1995	160	$2^{63}$	$2^{151.1}$ [KK12] 57/80 rounds
SHA-256	2001	256	$2^{65.5}$ 31/64 rounds	$2^{255.5}$ [KRS12] 45/64 rounds

# Hash Functions

Requirements for security and performance can vary on application.



Performance on  
long/short mes-  
sages.

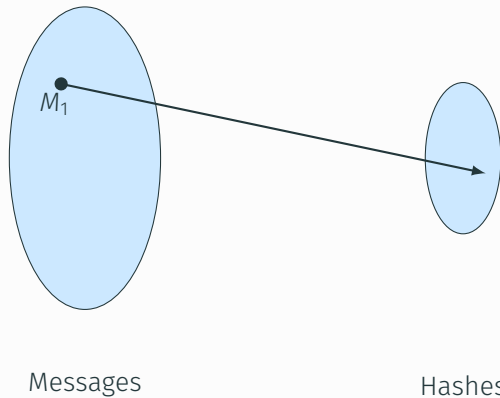
Password Hashing  
should be slow!



Collision resistance not  
required!

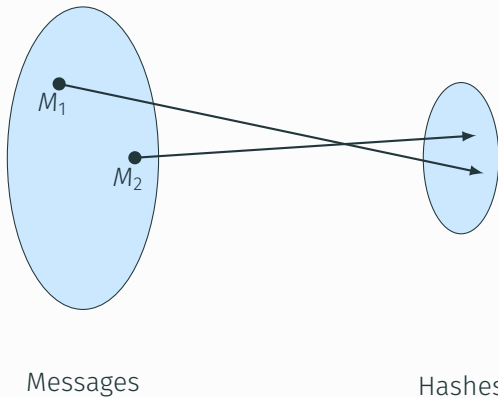
# Hash Functions

Ideal Hash Function



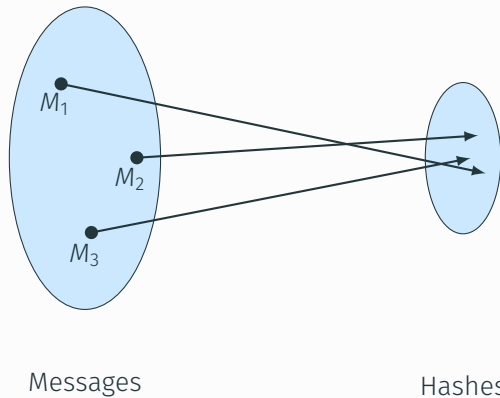
# Hash Functions

Ideal Hash Function



# Hash Functions

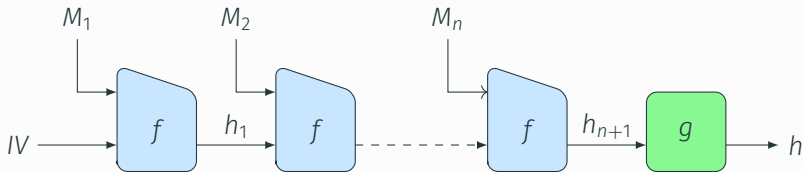
Ideal Hash Function



# Hash Functions

How to construct a hash function?

- Merkle-Damgård with compression function (SHA-1, SHA-2)



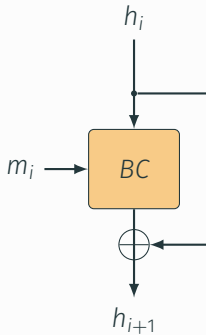
## Problem

How do we construct the compression function?

# Hash Functions

How to construct a hash function?

- Merkle-Damgård with compression function (SHA-1, SHA-2)

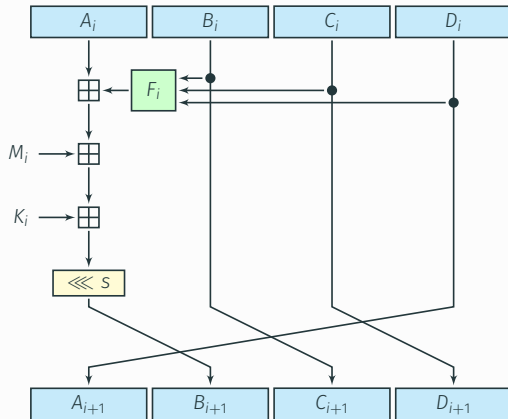


## Solution

Use a block cipher! ... but often state is too small.

# Hash Functions

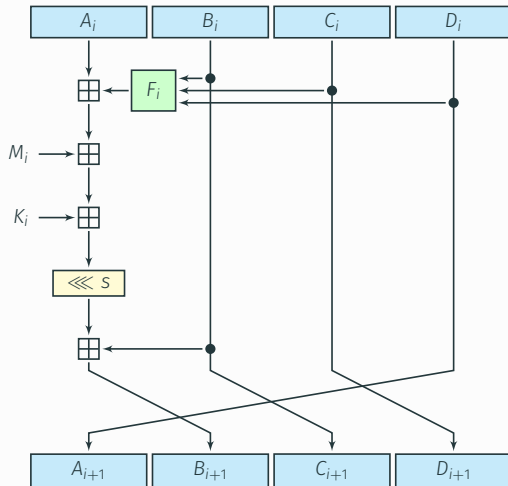
## Compression Function Design (MD4)



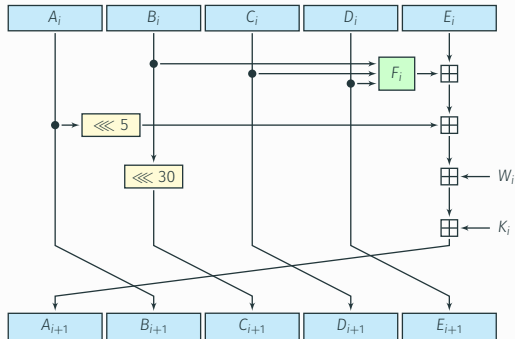


# Hash Functions

## Compression Function Design (MD5)

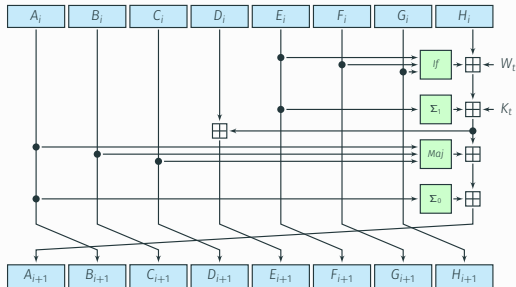


## Compression Function Design (SHA-1)



# Hash Functions

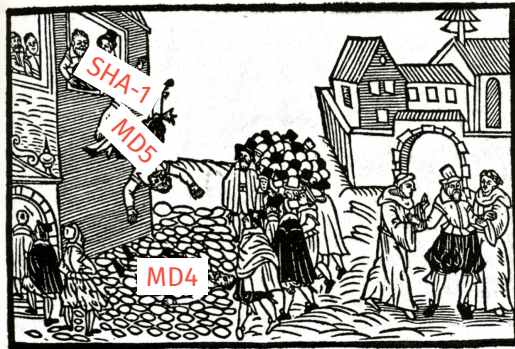
## Compression Function Design (SHA-2)



# Hash Functions

## The 2005 Hash Crisis

- Wang and Yu show that **MD5** is not collision resistant [WY05]...
- ... and **SHA-1** isn't either [WYY05].
- Concerns that SHA-2 will also fail.



## The SHA-3 Competition

- Public Competition to find a new standard SHA-3.
- From 2007 to 2012

- |                      |              |             |                 |
|----------------------|--------------|-------------|-----------------|
| • Abacus             | • ECHO       | • Lesamnta  | • SHAMATA       |
| • ARIRANG            | • ECOH       | • Luffa     | • SHAvite-3     |
| • AURORA             | • Edon-R     | • LUX       | • SIMD          |
| • Blake              | • EnRUPT     | • Maraca    | • Skein         |
| • Blender            | • ESSENCE    | • MCSSHA-3  | • Spectral Hash |
| • Blue Midnight Wish | • FSB        | • MD6       | • StreamHash    |
| • Boole              | • Fugue      | • MeshHash  | • SWIFFTX       |
| • Cheetah            | • Grøstl     | • NaSHA     | • Tangle        |
| • CHI                | • Hamsi      | • NKS2D     | • TIB3          |
| • CRUNCH             | • HASH 2X    | • Ponic     | • Twister       |
| • CubeHash           | • JH         | • SANDstorm | • Vortex        |
| • DCH                | • Keccak     | • Sarmal    | • WaMM          |
| • Dynamic SHA        | • Khichidi-1 | • Sgàil     | • Waterfall     |
| • Dynamic SHA2       | • LANE       | • Shabal    | • ZK-Crypt      |

# Hash Functions

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### • Blake

- Blender
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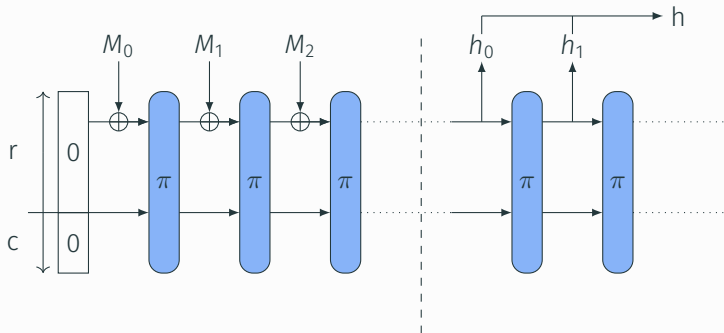
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# Hash Functions

## SHA-3 Winner Keccak

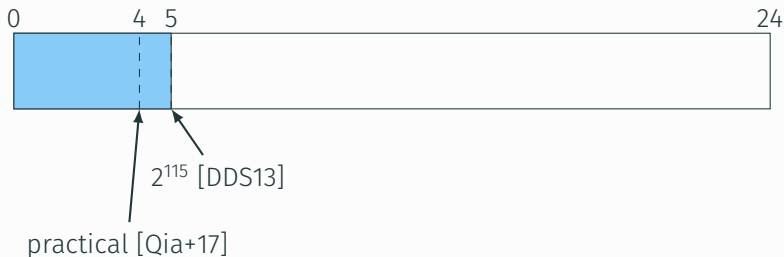


- Based on the sponge construction.
- Uses 1600-bit permutation  $\pi$ .
- Parameters: rate  $r$  and capacity  $c$ .
- Security claim of  $2^{c/2}$ .



# Hash Functions

SHA3-256 ( $c = 512$ ) collision resistance



Practical Attacks for  $c = 160^1$ :

- Collisions for 6 rounds
- Preimages for 4 rounds

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<sup>1</sup>[http://keccak.noekeon.org/crunchy\\_contest.html](http://keccak.noekeon.org/crunchy_contest.html)

# Hash Functions

What should you use now?

*"We don't need another slow, secure hash function—we've already got SHA-2."*

—Adam Langley, Mar. 2017<sup>2</sup>

SHA-3 standard too conservative?<sup>3</sup>

- Use different parameters.
- Tree hashing mode for better performance.
- RFC for Kangaroo12<sup>4</sup>



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<sup>2</sup><https://www.imperialviolet.org/2017/05/31/skipsha3.html>

<sup>3</sup>[http://keccak.noekeon.org/is\\_sha3\\_slow.html](http://keccak.noekeon.org/is_sha3_slow.html)

<sup>4</sup><https://tools.ietf.org/html/draft-viguier-kangarootwelve-00>

# Symmetric Key Cryptography

What can we do?

- Encryption
- Authentication (MAC)
- Hashing
- Random Number Generation
- Digital Signature Schemes
- Key Exchange



Questions?



Nadhem J. AlFardan et al. “On the Security of RC4 in TLS”. In: *Proceedings of the 22th USENIX Security Symposium*. 2013, pp. 305–320.



Johannes A. Buchmann, Erik Dahmen, and Andreas Hülsing. “XMSS - A Practical Forward Secure Signature Scheme Based on Minimal Security Assumptions”. In: *Post-Quantum Cryptography - 4th International Workshop, PQCrypto 2011, Taipei, Taiwan, November 29 - December 2, 2011. Proceedings*. 2011, pp. 117–129.



Andrey Bogdanov, Dmitry Khovratovich, and Christian Rechberger. “Biclique Cryptanalysis of the Full AES”. In: *Advances in Cryptology - ASIACRYPT 2011*. 2011, pp. 344–371.



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